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Test method

# Test methods for measuring pure mode III delamination toughness of composite

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## A B S T R A C T

This paper focuses on the characterization of pure mode III delamination behavior of composite materials. The development for pure mode III delamination testing methods is reviewed. Two testing methods for mode III experiments were evaluated: a novel test proposed in our previous study, termed Edge Ring Crack Torsion (ERCT) test, and the widely used Edge Crack Torsion (ECT) test. The two methods were compared by experiment and finite element analysis. The results demonstrate the advantage of ERCT. The limitations of the ECT test are discussed.

Keywords:

Mode III delamination

Testing method

Edge Ring Crack Torsion test (ERCT)

## 1. Introduction

Delamination is one of the common damage modes in a laminated composite. In order to establish a general criterion capable of representing the delamination resistance of a composite, one must know how to measure correctly the delamination toughness for each pure mode in terms of critical strain energy release rate. Currently, the characterization methods for delamination under pure mode I, pure mode II, as well as a mixed mode of I + II [1,2] have been widely studied. On the contrary, the work regarding the participation of mode III is quite limited because a pure mode III delamination is not easy to achieve in experiment. As a result, the mode III is usually considered as a shear mode the same as mode II, and the same critical strain energy release rate is assumed such that  $G_{IIc} = G_{IIIc}$ . However, this assumption is not satisfactory because the two shear modes are physically distinctive and the values of  $G_{IIc}$  and  $G_{IIIc}$  can be quite different for some composite materials.

Generally, a pure mode III delamination test should meet the following conditions:

- (1) the participation of mode I and mode II must be small enough to be negligible;
- (2) the variation of the strain energy release rate in mode III,  $G_{III}$ , along the crack front should be as small as possible so that its

average value at the crack onset can be regarded as the fracture toughness.

In literature, a number of test methods have been proposed for the evaluation of the mode III critical strain energy release rate,  $G_{IIIc}$ . The first tests introduced were the Crack Rail Shear test (CRS) (Becht and Gillespie, 1988) [3] and the Split Cantilever Beam test (SCB) (Donaldson, 1988) [4]. The main drawback of these tests is the participation of mode I and mode II in the area around the edges of the crack front [3–5].

The closed-form expression to determine  $G_{IIIc}$  from a SCB test is based on the beam theory, and the classical unidirectional specimens can be used in this test. Its configuration has been modified by different authors in order to cancel mode I and mode II, as well as to obtain a more uniform  $G_{III}$  along the crack front. In general, most modified SCB tests can eliminate the mode I component and reduce the mode II component. Robinson and Song [6] tried to limit the bending moment by introducing additional constraints, but they concluded that the experimental Compliance Calibration (CC) method could no longer be applied in the data reduction schema. Another modified version of SCB configuration (MSCB) was then realized by Sharif et al. [7], whose specimen was loaded by special grips and the mode II component was significantly reduced. The data reduction method based on an improved beam theory was found to be more reliable than the CC method [8]. However, the measurement of  $G_{IIIc}$  was disturbed because the specimen was strongly constrained at its edges near the crack front, so the variation of  $G_{III}$  along the crack front became more significant. As a

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result, it was not easy to define the crack onset at the load–displacement curves [9,10]. Later, a small free edge crack along the length of the specimens in the MSCB specimen test was introduced by Davidson and Sediles [11] in order to obtain a more uniform  $G_{III}$  along the crack front. The results highlighted the fact that the distribution of  $G_{III}$  along the crack front was fairly small. Moreover, the delamination onset was defined by a load drop even although a high level of non-linearity before the critical load was observed. However, the width of the edge crack along the specimen length had to be in several millimeters. It is difficult to guarantee such accuracy [11].

The Edge Crack Torsion (ECT) test was proposed by Lee (1993) [12]. A tensile machine was used to load the specimen under torsion up to delamination growth from an edge crack. The closed-form expression to determine  $G_{IIIc}$  was based on the plate theory. Different from SCB, the specimens have to be multidirectional laminates whose in-plane twisting stiffness and strength must be strong enough to assure the crack propagation. Actually, the loading conditions in the first ECT tests [12–17] were not symmetrical to the specimen axis, which induced a significant variation of  $G_{III}$  at one side of the crack front. Recent studies [18–24] adopted a configuration with more symmetric loading conditions. This modification allows decreasing the likelihood of geometric nonlinearity and improving the uniformity of  $G_{III}$  along the crack front. Another ECT configuration using a torsion machine, called ECT-a thereafter, was proposed by H. Suemasu [25] aiming at obtaining uniform distribution of  $G_{III}$  along the crack front. Both ends of specimens in the ECT-a test were loosely fixed so that an axial sliding was permitted during the application of an axial torque. In all ECT tests, pure mode III component proved to be in the mid-region of crack front, while mode II component appears near the edges. Mode II component can be reduced to a reasonable level with an appropriate choice of the specimen geometry [18–20,22]. It is not satisfactory to apply the data reduction schema based on experimental CC method for determining  $G_{IIIc}$  because a large number of specimens with different initial crack lengths had to be used, and the value of  $G_{IIIc}$  was found to increase with the crack length [22]. Moreover, small initial crack lengths for ECT specimens should be preferable for measuring  $G_{IIIc}$  [26], but too small initial crack lengths would decrease the accuracy because of the uncertainty in the real crack length measurement. Furthermore, it is not easy to identify the crack onset in most ECT tests because there is a significant non-linearity on the load/displacement curve before the critical load is reached, which can be associated with a R-curve effect [18–22,27–29]. Recently, a Six-Point Edge Crack Torsion (6ECT) test was proposed by Pereira et al. [30], who contribute to a relatively clear identification of the critical load and evaluation of the mode III R-curve effect.

Unfortunately it can be seen that the participation of mode II in all these tests can never be totally eliminated. In most cases, the variation of  $G_{III}$  along the crack front is too big to be negligible. Generally, this variation is smaller in the central region of the crack front, but much more significant at the edges.  $G_{III}$  values can go to almost zero at the two edges of the crack front. To reduce the influence of this edge effect it is better to use specimens with a longer crack front. Compared to SCB test, the crack front length of the ECT specimen is less limited.

In summary, a test method for the characterization of pure mode III delamination is yet to be developed. Recently, an original pure mode III test has been proposed, termed Edge Ring Crack Torsion (ERCT) test [31]. This is a torsion test on a composite plate containing an edge ring crack between two layers. The loading mode obtained is pure mode III, and the crack front is circular, i.e. it is closed without edges. The edge effect in ECT specimens mentioned above is, therefore, eliminated. Moreover, the variation

of  $G_{III}$  along the crack front can be reduced by optimizing different parameters of the specimen and the testing device.

In order to further validate the ERCT method, this paper compares the ERCT with the ECT-a test method. The mode III experiments were conducted with a carbon/epoxy composite. Finite element analysis (FEA) for the two testing methods was performed.

## 2. Experimental

### 2.1. Materials and specimens

All specimens for ERCT and ECT tests were obtained from a woven carbon/epoxy taffeta fabric prepreg (ref: IMP503Z). Table 1 lists the properties of the unidirectional composite, i.e. a laminate with yarns oriented in  $0^\circ$  in all fabric plies.

The composite laminate was manufactured by hand lay-up and a 13  $\mu\text{m}$  thick polyester film was inserted in the mid-thickness of the laminate in order to create a pre-crack. 32 plies were used for the whole laminate and the stacking sequence was [0/45/45/0/45/0/0/45/45/0/0/45/0/45/45/0]//crack//[0/45/45/0/45/0/0/45/45/0/0/45/0/45/45/0], where 0 represents a taffeta balanced fabric ply with yarns oriented in  $0^\circ$  and  $90^\circ$ , while 45 represents the same fabric oriented at  $\pm 45^\circ$ . The pre-crack symmetrically separates the laminate into two sub-laminates, which are also symmetrical laminates relative to their midplanes.

The stacking sequence of each sub-laminate was optimized in order to obtain particular laminate characteristics:

- quasi-homogeneous, i.e. the same elastic stiffness properties in tension and in bending;
- quasi-isotropic, i.e. the same elastic stiffness properties in tension and in bending in all direction;
- the elimination of all possible coupling terms:  
 $B_{ij} = A_{16} = A_{26} = D_{16} = D_{26} = 0$

The crack front of ERCT specimen is circular (Fig. 1(a)) whereas that of ECT-a is rectilinear (Fig. 1(b)). For the former, a disc was cut out in the center of the inserted polyester film with the help of a circle cutter. The circular hole of diameter  $d$  forms a non-delaminated area (Fig. 1(a)). In order to locate the center of the circular hole on the rotation axis of the machine, the center of the hole is identified on the outer skins of the sample. The precise location of the hole has been verified by Ultrasonic C-scan.

### 2.2. Test methods

All the tests were carried out at ambient temperature. An axial rotation speed of  $0.5^\circ/\text{min}$  was imposed.

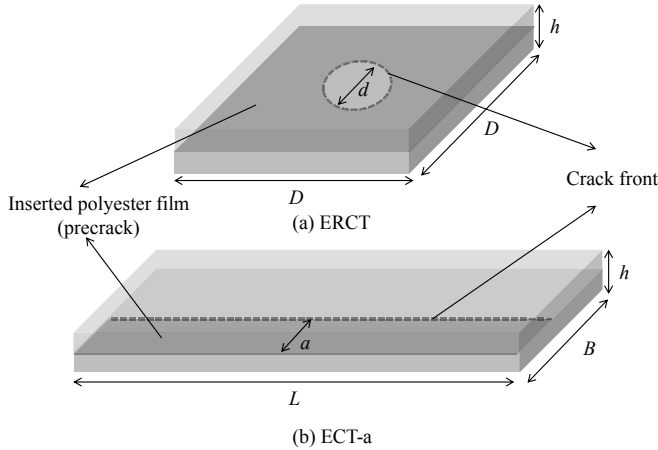
Concerning the ERCT tests, two diameters  $d$  of the central circle (non-delaminated area) were used while the outer diameter of the ring crack was kept the same. In ECT tests, specimens with 4 different initial crack lengths were tested for the application of CC method. The dimensions of all specimens tested are listed in Table 2.

#### 2.2.1. Edge Ring Crack Torsion test (ERCT)

ERCT (Fig. 2) was proposed in order to obtain pure mode III delamination. Firstly, the composite specimen was pasted to the ring protruding from two rigid plates. The inner and outer diameters of the ring;  $d_{ring}$  and  $D_{ring}$ , were 80 mm and 120 mm respectively. Great care was taken in order to locate the center of the circular non-delaminated area on the axis of the rigid plates during the pasting process. Secondly, the rigid plates were screwed to the torsion device. Finally, the torsion device was submitted to an imposed rotation up to the crack propagation. As a result of the

**Table 1**  
Properties of the unidirectional laminate used.

|  |                         |
|--|-------------------------|
| Fabric weight  | 200 (g/m <sup>2</sup> ) |
| Glass transition temperature: $T_g$                    | 120 (°C)                |
| Percentage of matrix: $V_m$                            | 42%                     |
| Longitudinal and transverse modulus: $E_{11} = E_{22}$ | 55250 (MPa)*            |
| Out-of-plane shear modulus: $G_{13} = G_{23}$          | 5400(Mpa)*              |
| Tensile strength in direction 1 and 2: $X^+ = Y^+$     | 669 (MPa)*              |
| Poisson's ratio 12: $\nu_{12}$                         | 0.044*                  |
| Shear modulus in direction 12: $G_{12}$                | 4062 (MPa)*             |
| Shear strength in direction 12: $S_{12}$               | 117 (MPa)*              |



**Fig. 1.** Schematics of the specimens with inserted polyester film for (a) ERCT and (b) ECT-a.

holes in the rigid plates, it was also possible to observe the crack propagation by Ultrasonic C-scan.

### 2.2.2. Edge Crack Torsion test (ECT-a)

In ECT-a test, both ends of the test specimens were blocked in jaws and an axial sliding was permitted by the machine during the application of a torque, shown in Fig. 3. Note that no extra device is required.

## 3. Finite element analysis

FEA was performed using Ls-Dyna, a commercial FE package. The devices and the specimens were modeled with 3D solid elements. MAT 22, a material model based on the Chang-Chang fracture criterion, was chosen to simulate the composite laminates. Spring elements were arranged at the crack tip along the crack front in order to obtain local loads and relative displacements, which are necessary to determine the value of  $G_I$ ,  $G_{II}$ , and  $G_{III}$  by the virtual crack closure technique (VCCT) [32; 33]. The surface to surface contact was applied on the two delamination surfaces to prevent interpenetration during the analysis. The relative sliding between the points within the delamination plane was assumed to be frictionless.

In the FE model, each ply was modeled with one layer of sold element with its orientation defined according to the stacking sequence. The principal properties of material were set according to

**Table 2**  
Geometries of the specimens of ERCT and ECT-a.

|            |         |                 |                  |                   |
|------------|---------|-----------------|------------------|-------------------|
| ERCT (mm)  | $h = 7$ | $d_{ring} = 80$ | $D_{ring} = 120$ | $d = 30,50$       |
| ECT-a (mm) | $h = 7$ | $L = 150$       | $B = 40$         | $a = 10,15,20,25$ |

Table 1, where all values with “\*” were measured on unidirectional laminate used while others were referred to the literature.

The FE mesh close to the crack front was locally refined (Fig. 4) to guarantee good accuracy of the results. The mesh refinement has been studied. It demonstrated that the difference on  $G_i$  ( $i = I, II, III$ ) calculated by VCCT between the model with the current mesh and that with twice numbers of elements in the plate plane ( $r, \theta$ ) near the crack front is about 1%. Concerning the thickness direction  $z$ , a model with two elements in the thickness of each ply of the plate has been tested on a simplified model loaded in torsion, and leads to 2.7% of variation. However, the quality of the finite element is degraded by refining the mesh in the  $z$  direction, because its aspect ratio, i.e. the dimension in  $z$  is too small compared to those in  $r$  and  $\theta$  directions.

As an example, the FE model used for ERCT is shown in Fig. 5, where  $\theta$  is defined in a polar coordinate. ECT-a test model is shown in Fig. 6. Note that the position of the ECT-a specimen relative to the torsional axis influences the distribution of  $G_{III}$ . The FEA of ECT-a test also allows optimizing the position of the specimen in the jaws in order to obtain the crack onset from the pre-crack, but not from the opposite edge. Actually, it would be better to place the crack front close to the rotation axis.

## 4. Results and discussion

### 4.1. Edge Ring Crack Torsion test (ERCT)

In the ERCT test, the edge ring crack grows towards the center of the non delaminated area and always in an unstable manner. The test reproducibility is fairly good. Fig. 7 shows a typical experimental torque-rotation curve, where a sudden drop in the torque is observed after a small nonlinear part. In this study, the peak torque is considered as the critical load,  $T_C$ , corresponding to the crack growth onset. Actually, we could not stop the test in the nonlinear area to know whether the crack has propagated. The test was stopped right after the load drop, and then the specimen was scanned by Ultrasonic C-scan in order to verify the crack propagation.

Fig. 8 shows the images obtained by Ultrasonic C-scan on the three tested specimens with  $d = 30$  mm before and after crack growth, where the white zone presents the non-delaminated area. It demonstrates that the crack indeed propagated. Moreover, it seems that the crack propagated much more along an angle  $\theta_C$  close to ( $\pm 45^\circ$ ). One explanation may be that the crack resistance varies as a function of the adjacent fiber directions, and the resistance of the crack tips at  $\theta_C$  is smaller under shear mode. We can also imagine that the penetration of air and/or water into the delaminated areas after the test depends on their fracture mode and damage level. To verify these assumptions, the interpretation of the images obtained from Ultrasonic C-scan requires further study.

The curves in Fig. 9 and Fig. 10 illustrate the evolution of  $G_I$ ,  $G_{II}$  and  $G_{III}$  along the crack front obtained by finite element method at the critical torque  $T_C$ . It is interesting to note that the contributions of mode I and mode II are almost zero, which demonstrates that the crack is indeed loaded in pure mode III. The values of  $G_{III}$  show a periodic variation instead of being constant which, however, can be minimized by optimization,. In fact, the evolution of  $G_{III}$  along the crack front is the result of different influences. It depends, not only on the geometry of the device used for applying the torque, which is not strictly axisymmetrical, but also on the composite specimens, especially on the adjacent fiber orientation relative to the local crack front. The ratio of  $d/D_{ring}$  is also a parameter that determines the importance of the effects mentioned above. If we define a relative variation parameter as follows:  $\Delta = |G_{III-max} - G_{III-av}| / G_{III-av}$ , and  $\Delta$  is about 7.5% for the specimens with  $d = 30$  mm and 17.4% for

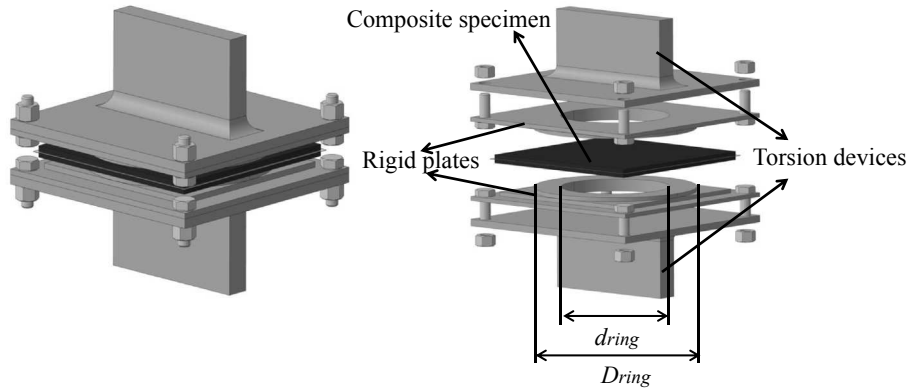


Fig. 2. Edge Ring Crack Torsion test device (ERCT).

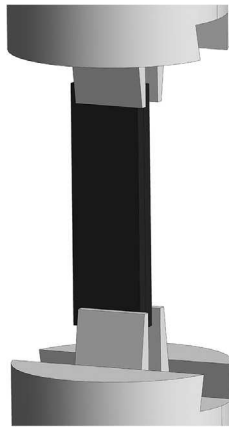


Fig. 3. Configuration of Edge Crack Torsion-2 test (ECT-a).

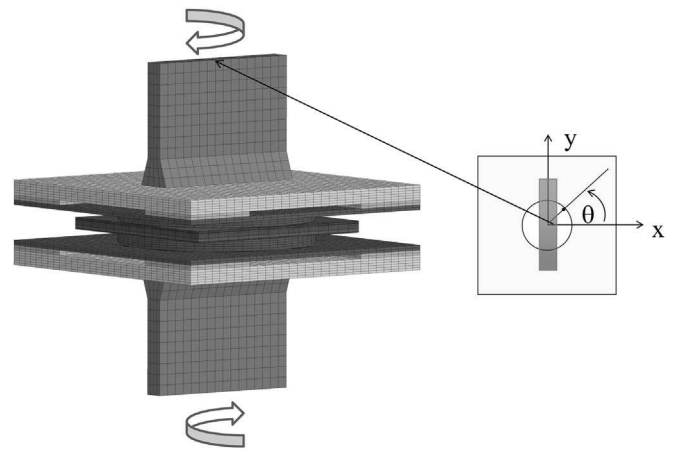


Fig. 5. Finite element model of the ERCT test.

those with  $d = 50$  mm. Moreover, the maximum  $G_{III}$  is localized at  $\theta = 0^\circ$  and  $180^\circ$ , so the propagation of the crack should initiate at these crack tips if the toughness in pure mode III was independent of adjacent fiber orientation. A simply and practical approach was then considered. In the case of an infinite cylinder of diameter  $D$  including an edge ring crack at a cross section submitted to an axial torque  $T$ , where the crack front is circular of diameter  $d$ , the stress

intensity factor  $K_{III}$  is given by a semi-analytical Equation (1) from the Tada Handbook [34].

$$K_{III} = \frac{16T}{\pi d^3} \sqrt{\pi \frac{(D-d)}{2}} \cdot f\left(\frac{d}{D}\right) \quad (1)$$

$$\text{with } f\left(\frac{d}{D}\right) = \frac{3}{8} \sqrt{\frac{d}{D}} \left[ 1 + \frac{1}{2} \frac{d}{D} + \frac{3}{8} \left(\frac{d}{D}\right)^2 + \frac{5}{16} \left(\frac{d}{D}\right)^3 + \frac{35}{128} \left(\frac{d}{D}\right)^4 + 0,208 \left(\frac{d}{D}\right)^5 \right]$$

In fracture mechanics,  $K_{III}$  is related to strain energy release rate  $G_{III}$  by Equation (2) for isotropic materials if the crack grows in a self-similar manner, where  $G$  is the shear modulus of the isotropic material.

$$G_{III} = \frac{1}{2G} K_{III}^2 \quad (2)$$

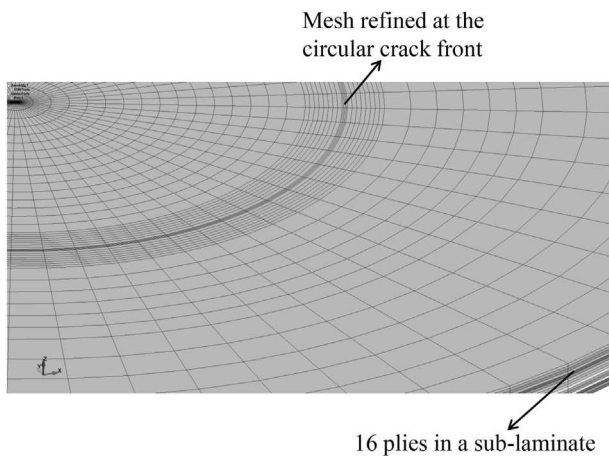


Fig. 4. Finite element mesh of the ERCT specimen.

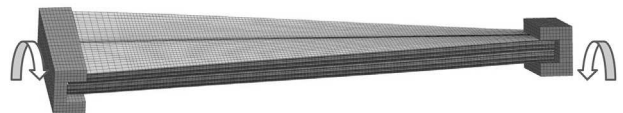


Fig. 6. Finite element model of the ECT-a test.

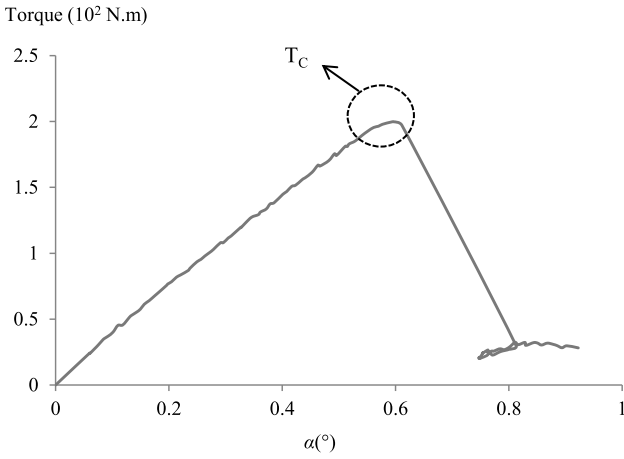


Fig. 7. A typical experimental torque-rotation curve of ERCT test with  $d = 30$  mm.

Actually, the FE model was also validated by comparison of the calculated  $G_{III}$  using VCCT and Tada formula, which are obtained from an isotropic cylinder model. The difference is less than 2%. Herein, the isotropic cylinder is in steel with length of  $2 \times 50$  mm and diameter of 120 mm. An edge ring crack is located at mid-length, whose non cracked area has a diameter of 30 mm. It is interesting to note that, although the cylinder simulated here is not really an infinite cylinder, the Tada's formula seems to be a good approach for an isotropic material.

Even although the crack in ERCT specimens is embedded in two plates in laminated composite instead of an isotropic cylinder, we want to know whether this closed-form formula can be applied for determining  $G_{III}$  in the case of the ERCT test. Note that  $G$  calculated by Equation (2) should be  $G_{z\theta}$  for a laminate, which generally varies as a function of  $\theta$ . However, the tested laminates are quasi-isotropic. So  $G_{z\theta}$  is constant and  $G_{z\theta} = G_{13}$  according to the analysis by J.M. Berthelot [35]. By introducing the critical torque into the Equations (1) and (2), the toughness in pure mode III can be obtained. Table 3 gives the results for the specimens with  $d = 30$  mm and  $d = 50$  mm. The difference of  $G_{IIIc}$  is small, so no significant influence of the crack diameter on  $G_{IIIc}$  was observed.

As a result, the average value of  $G_{IIIc}$  will be considered, named

$G_{IIIc-Tada}$ . It is presented in the same table and also compared to the numerical results in Figs. 9 and 10. It is shown that, for the specimen with  $d = 30$  mm, the  $G_{IIIc-Tada}$  value agrees well with the average value calculated at the critical load by VCCT, named  $G_{IIIc-FEM}$ . The difference between  $G_{IIIc-Tada}$  and  $G_{IIIc-FEM}$  measured on the specimens with  $d = 30$  mm is only approximately 2.2%; this difference is more significant measured on those with  $d = 50$  mm, which is approximately 20.5%. It seems that if the variation of  $G_{III}$  along the crack front is large, the closed-form proposed by Tada would no longer be applicable.

#### 4.2. Edge Crack Torsion test (ECT-a)

Fig. 11(a) gives a typical experimental curve of the ECT-a test. Herein, the critical load corresponding to the onset of crack growth is not easy to define. We try to define an appropriate critical torque  $T_C$  in different ways. Three values of  $G_{IIIc}$  were calculated according to different definitions of  $T_C$ :  $T_{C-1}$  is the torque at the end of the linear domain;  $T_{C-2}$  the torque at the intersection of the curve and a line at 90% of initial slope of the linear domain;  $T_{C-3}$  the torque at first visible drop in the torque value.

Firstly, one of the three tests was stopped and scanned right after the first drop in torque ( $T_{C-3}$ ), shown in Fig. 11(b). Not only the propagation at the pre-crack was observed, but also a little propagation at the opposite edge, where the expression proposed for determination of  $G_{IIIc}$  is no longer available. We believe that the onset of crack occurs before reaching  $T_{C-3}$ . The critical torque is believed to be between  $T_{C-1}$  and  $T_{C-2}$ . Similar conclusions were reached in the work of Marat-Mendes R [21].

The evolution of  $G_I$ ,  $G_{II}$  and  $G_{III}$  along the crack front computed at  $T_{C-2}$  for ECT-a specimen with initial crack length of 20 mm is illustrated in Fig. 12. It is seen that the uniformity of  $G_{III}$  in ECT-a test is better in the central domain along the crack front, but the values of  $G_{III}$  drop dramatically at the edges ( $x/L = 0$  and 1). However, the value of  $\Delta$  is about 14.0%, close to that from ERCT specimens with  $d = 50$  mm. Moreover, the loading condition is a mixed mode III+ $\Delta$ II at the crack edges. For the specimens with other initial crack length, the distribution of  $G_I$ ,  $G_{II}$  and  $G_{III}$  along the crack front is similar.

Aiming at finding a simple and practical approach, the critical strain energy release rate was then calculated using CC method (Equation. (4)) modified from Equation (3) [21], where  $C$  is the

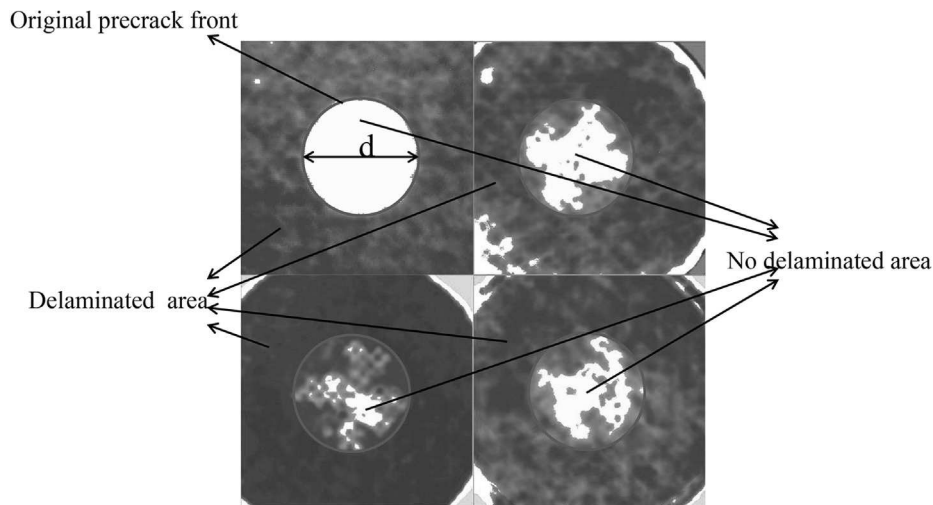


Fig. 8. Ultrasonic C-scan images before and after propagation on the three ERCT specimens with  $d = 30$  mm.

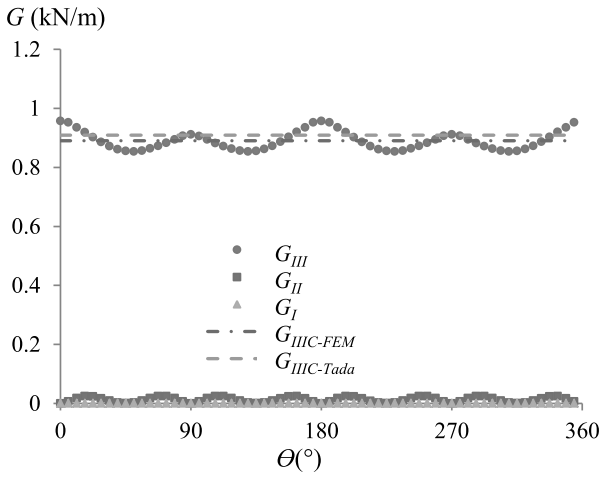


Fig. 9. Evolution of  $G_I$ ,  $G_{II}$  and  $G_{III}$  along the circular crack front of ERCT specimen with  $d = 30$  mm.

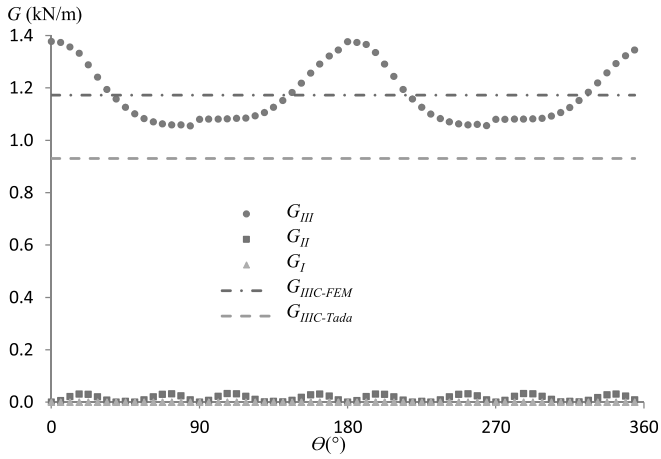


Fig. 10. Evolution of  $G_I$ ,  $G_{II}$  and  $G_{III}$  along the circular crack front of ERCT specimen with  $d = 50$  mm.

measured compliance and  $m$  is obtained by the compliance calibration.

$$G_{III} = \frac{mCP_c^2}{2BL \left(1 - m\left(\frac{a}{B}\right)\right)} \quad (3)$$

$$G_{III} = \frac{mCT^2}{2BL \left(1 - m\left(\frac{a}{B}\right)\right)} \quad (4)$$

The results are compared in the Fig. 13. It is seen that the values of  $G_{III}$  measured on the specimens with different initial crack lengths (10 mm, 15 mm, 20 mm, 25 mm) are very close to each other if  $T_{C-1}$  or  $T_{C-2}$  are considered as the critical load while the

Table 3  
 $G_{III}$  obtained from Tada's formula for ERCT tests.

| $d$ (mm) | $T_{C-av}$ (N.m) | $G$ (MPa) | $K_{III}$ (MPa.m <sup>1/2</sup> ) | $G_{III-Tada}$ (N/m) |
|----------|------------------|-----------|-----------------------------------|----------------------|
| 30       | 204 ± 4          | 5400      | 3.13 ± 0.06                       | 910 ± 34             |
| 50       | 742 ± 3          | 5400      | 3.17 ± 0.02                       | 932 ± 11             |

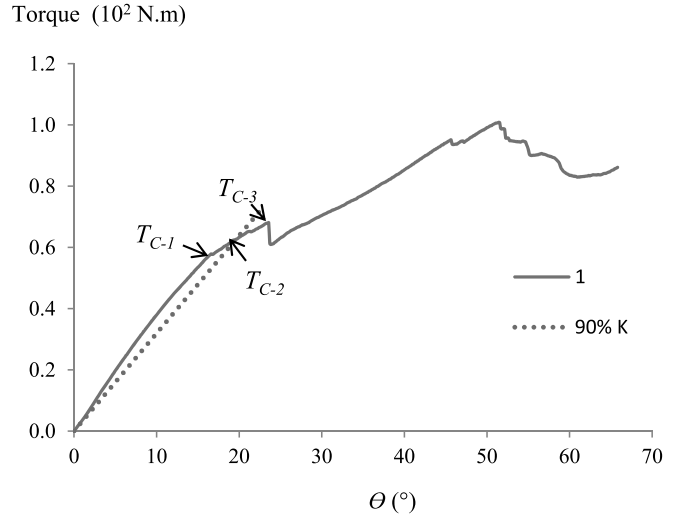


Fig. 11. A typical experimental torque-rotation curve and the Omniscan image of ECT-a test (a) Definitions of critical load (b) Omniscan image for one specimen.

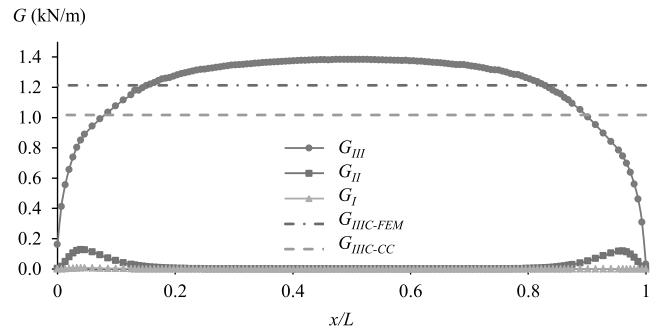


Fig. 12. Evolution of  $G_I$ ,  $G_{II}$  and  $G_{III}$  along the crack front of ECT-a specimen.

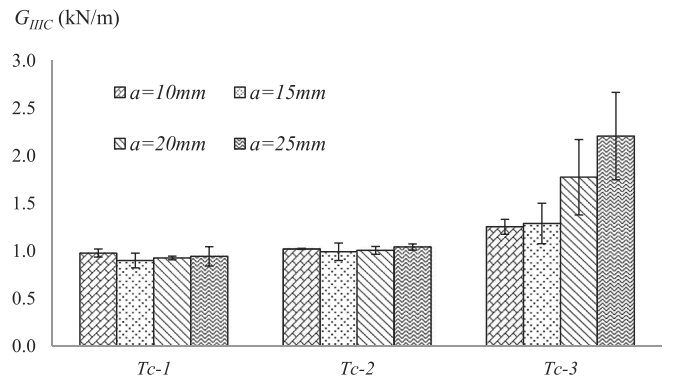


Fig. 13. Comparison of  $G_{III}$  results with ECT-a test.

difference becomes too large if  $T_{C-3}$  is used. Actually, the  $G_{III}$  using  $T_{C-3}$  corresponds to the first unstable crack propagation instead of the onset of crack growth, and the definition of the value of  $T_{C-2}$  is more meaningful experimentally. Therefore, only  $T_{C-2}$  is used to determine  $G_{III}$  for discussion in next section.

Finally, the average value of  $G_{III}$  from all the tests with specimen  $a = 20$  mm obtained by Equation (4), named  $G_{III-CC}$ , are also presented in Fig. 12. It shows that  $G_{III-CC}$  is 16.2% smaller than  $G_{III-FEM}$ .



**Table 4**Comparison of  $G_{IIIc}$  obtained from two mode III tests.

| Type of test         | $G_{IIIc-FEM}$ (N/m) | $G_{IIIc-Tada}$ or $G_{IIIc-CC}$ (N/m) | $(G_{IIIc-Tada} - G_{IIIc-FEM})/G_{IIIc-FEM}$ or $(G_{IIIc-CC} - G_{IIIc-FEM})/G_{IIIc-FEM}$ |
|----------------------|----------------------|--|--|
| ERCT ( $d = 30$ mm)  | 890 ± 32             | 910 ± 34                               | 2.2%   |
| ERCT ( $d = 50$ mm)  | 1173 ± 110           | 932 ± 11                               | 20.5%  |
| ECT-a ( $a = 20$ mm) | 1213 ± 264           | 1017 ± 44                              | 16.2%  |

## 5. Conclusion

After the review of the development of pure mode III testing methods, it is found that most of the tests proposed in the literature cannot completely eliminate the contribution of mode II. Furthermore, the distribution of  $G_{III}$  along the crack front is far from uniform. As a result, the test method for the determination of  $G_{IIIc}$  should be improved.

In this study, the novel test ERCT and the ECT-a test were performed on a woven carbon/epoxy taffeta composite. These tests were also simulated using FEA to investigate the evolution of  $G_I$ ,  $G_{II}$  and  $G_{III}$  along the crack front. The values of  $G_{IIIc}$  obtained by different methods for the two tests are listed in Table 4. For both tests, the results of FEA show that the data reduction methods based on average value may not be good enough to determine the toughness if the variation of  $G_{III}$  along the crack front is significant because the value of  $G_{IIIc-FEM}$  can be much higher than that from the other simplified approaches. It is interesting to note that the relative variation parameter  $\Delta$  and the maximum value of  $G_{III-max}$  for ERCT test with  $d = 50$  mm is close to that from ECT-a test.

The most significant advantages of ERCT test are:

- the fracture mode is pure mode III without contributions of mode I or mode II components;
- the variation of  $G_{III}$  along the crack front is much smaller than ECT tests;  $\Delta$  can be less than 7.6% by optimizing the geometry of the specimen. Hence, it is acceptable to consider the average value as the material toughness;
- the critical load corresponding to the crack onset is easy to define;
- the agreement between  $G_{IIIc-Tada}$  and  $G_{IIIc-FEM}$  is good for a small diameter  $d$ .

Some limitations of ERCT test must be mentioned:

- the crack resistance may vary as a function of the adjacent fiber orientations. If that is the case, the crack resistance is not a constant in ERCT test because the angle between fiber orientation and crack front varies regularly. In this case, the delamination toughness evaluated by Tada formula presents the smallest value, which is also meaningful
- the crack propagation is unstable, which prevents R-curve measurements

The limitation of the ECT-a test are:

- there is a participation of mode II component at the edges of the crack front;
- the variation of  $G_{III}$  along the crack front is significant when the whole crack front is taken into consideration because the values of  $G_{III}$  drop dramatically at the edges;
- the critical load corresponding to the crack onset is not easy to define;
- $G_{IIIc-CC}$  is 16.2% smaller than  $G_{IIIc-FEM}$ .

In conclusion, the ERCT test is a promising pure mode III test

method for measuring  $G_{IIIc}$ . It presents the best result so far in terms of eliminating mode I and II components and reducing the  $G_{III}$  variation along the crack front. However, further improvement of the ERCT test is still possible by investigating the factors affecting the evolution of  $G_{III}$  along the crack front, conducting a sensitivity study to experimental defaults, developing a more adequate closed-form expression for determining  $G_{IIIc}$  and improvement of the testing device.

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